Benha University<br>Faculty of Engineering (Shoubra)<br>Mechanical Engineering Department

1. A one dimentional plate of aluminum $\left(\mathrm{k}=100 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \rho=2700 \mathrm{~kg} / \mathrm{m}^{3}, \mathrm{C}=900 \mathrm{~J} / \mathrm{kg}^{\circ} \mathrm{C}\right) 1$ cm thick and initially at $200^{\circ} \mathrm{C}$ is suddenly exposed to air environment at $\mathrm{T}_{\infty}=30^{\circ} \mathrm{C}$ and convection heat transfer coefficient of $500 \mathrm{~W} / \mathrm{m}^{2} \mathrm{~K}$. Calculate the plate temperature 1 min after the plate has been exposed to the environment. How much energy has been removed per unit area from the plate at this time?
2. Consider an iron whose base plate is made of 0.5 cm -thick aluminum alloy $2024-\mathrm{T} 6\left(\rho=277 \mathrm{~kg} / \mathrm{m}^{3}, \mathrm{C}=875\right.$ $\mathrm{J} / \mathrm{kg}{ }^{\circ} \mathrm{C}, \alpha=7.3 \times 10^{-5} \mathrm{~m}^{2} / \mathrm{s}$ ). The base plate has a surface area of $0.03 \mathrm{~m}^{2}$. Initially, the iron is at $140^{\circ} \mathrm{C}$ in thermal equilibrium with the ambient air at $22^{\circ} \mathrm{C}$. Taking the heat transfer coefficient at the surface of the base plate to be $12 \mathrm{~W} / \mathrm{m}^{2}{ }^{\circ} \mathrm{C}$, determine how long it will take for the plate temperature to reach $80^{\circ} \mathrm{C}$ after turning it off. Is it realistic to assume the plate temperature to be uniform at all times?

3. Stainless steel ball bearings $\quad\left(\rho=8085 \mathrm{~kg} / \mathrm{m}^{3}, \mathrm{k}=\right.$ $15.1 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \mathrm{C}=0.480 \mathrm{~kJ} / \mathrm{kg}^{\circ} \mathrm{C}$, and $\alpha=3.91 \times 10^{-6} \mathrm{~m}^{2} / \mathrm{s}$ ) having a diameter of 1.2 cm are to be quenched in water. The balls leave the oven at a uniform temperature of $900^{\circ} \mathrm{C}$ and are exposed to air at $30^{\circ} \mathrm{C}$ for a while before they are dropped into the water. If the temperature of the balls is not to fall below $850^{\circ} \mathrm{C}$ prior to quenching and the heat transfer coefficient in the air is $125 \mathrm{~W} / \mathrm{m}^{2}{ }^{\circ} \mathrm{C}$, determine how long they can stand in the air before being dropped into the water. If 2500 balls are to be quenched per hour, determine the total rate of heat transfer from the balls to the
 air.
4. A thermocouple junction $\left(\mathrm{k}=20 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \mathrm{C}=400 \mathrm{~J} / \mathrm{kg}{ }^{\circ} \mathrm{C}\right.$ and $\left.\rho=5000 \mathrm{~kg} / \mathrm{m}^{3}\right)$ which may be approximated as a sphere is to be used for temperature measurement in a gas stream. The convection coefficient between the junction and the gas is known to be $\mathrm{h}=400 \mathrm{~W} / \mathrm{m}^{2}{ }^{\circ} \mathrm{C}$. Determine the junction diameter needed for the thermocouple to have a time constant of 1 s . If the junction is at $25^{\circ} \mathrm{C}$ and is placed in a gas stream that is $200^{\circ} \mathrm{C}$, how long will it take for the junction to reach $199^{\circ} \mathrm{C}$ ? Calculate total capacity heat.
5. A person is found dead at 5 PM in a room whose temperature is $20^{\circ} \mathrm{C}$. The temperature of the body is measured to be $25^{\circ} \mathrm{C}$ when found, and the heat transfer coefficient is estimated to be $\mathrm{h}=8 \mathrm{~W} / \mathrm{m}^{2}{ }^{\circ} \mathrm{C}$. Modeling the body as a 30 cm -diameter, 1.7 m -long cylinder ( $\rho=$ $996 \mathrm{~kg} / \mathrm{m}^{3}, \mathrm{k}=6 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \mathrm{C}=4109.3 \mathrm{~J} / \mathrm{kg}^{\circ} \mathrm{C}$ ). If The person was healthy before death with a body temperature of $37^{\circ} \mathrm{C}$, estimate the time of death of that person.
6. In a production facility, 4 - cm -thick large brass plates $\left(\mathrm{k}=110 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \rho=8530 \mathrm{~kg} / \mathrm{m}^{3}, \mathrm{C}=\right.$ $377 \mathrm{~J} / \mathrm{kg}{ }^{\circ} \mathrm{C}$, and $\alpha=33.9 \times 10^{-6} \mathrm{~m}^{2} / \mathrm{s}$ ) that are initially at a uniform temperature of $20^{\circ} \mathrm{C}$ are heated by passing them through an oven maintained at $500^{\circ} \mathrm{C}$. The plates remain in the oven for a period of 7 min . Taking the convection heat transfer coefficient to be $\mathrm{h}=120 \mathrm{~W} / \mathrm{m}^{2}{ }^{\circ} \mathrm{C}$, determine the surface temperature of the plates when they come out of the oven.
7. A large plate of aluminum $\left(\mathrm{k}=100 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \rho=2700 \mathrm{~kg} / \mathrm{m}^{3}, \mathrm{C}=900 \mathrm{~J} / \mathrm{kg}^{\circ} \mathrm{C}\right) 5-\mathrm{cm}$ thick and initially at $200^{\circ} \mathrm{C}$ is suddenly exposed to air environment at $\mathrm{T}_{\infty}=70^{\circ} \mathrm{C}$ and convection heat transfer coefficient of $525 \mathrm{~W} / \mathrm{m}^{2} \mathrm{~K}$. Calculate the temperature at a depth of 0.625 cm from one of the faces 1 min after the plate has been exposed to the environment. How much energy has been removed per unit area from the plate at this time?
8. A large aluminum (2024-alloy) plate ( $\mathrm{k}=177 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \rho=2770 \mathrm{~kg} / \mathrm{m}^{3}$ and $\mathrm{C}=875 \mathrm{~J} / \mathrm{kg}^{\circ} \mathrm{C}$ ) of thickness 0.15 m , initially at a uniform temperature of 300 K , is placed in a furnace having an ambient temperature of 800 K for which the convection heat transfer coefficient is estimated to be $500 \mathrm{~W} / \mathrm{m}^{2}{ }^{\circ} \mathrm{C}$. (a) Determine the time required for the plate mid plane to reach 700 K . (b) What is the surface temperature of the plate for this condition?
9. A long 20 -cm-diameter cylindrical shaft ( $\mathrm{k}=50 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \rho=8000 \mathrm{~kg} / \mathrm{m}^{3}, \mathrm{C}=500 \mathrm{~J} / \mathrm{kg}{ }^{\circ} \mathrm{C}$ ) comes out of an oven at a uniform temperature of $600^{\circ} \mathrm{C}$. The shaft is then allowed to cool slowly in an environment chamber at $200^{\circ} \mathrm{C}$ with an average heat transfer coefficient of $\mathrm{h}=$ $100 \mathrm{~W} / \mathrm{m}^{2}{ }^{\circ} \mathrm{C}$. Determine the temperature at the center of the shaft 45 min after the start of the cooling process. Also, determine the heat transfer per unit length of the shaft during this time period.
10. A large aluminum rod 5 cm in diameter and thermo-physical properties $\mathrm{k}=125 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \rho=$ $2700 \mathrm{~kg} / \mathrm{m}^{3}$, and $\mathrm{C}=900 \mathrm{~J} / \mathrm{kg}{ }^{\circ} \mathrm{C}$ is initially at a uniform temperature of $200^{\circ} \mathrm{C}$. It is suddenly exposed to air environment at $\mathrm{T}_{\infty}=70^{\circ} \mathrm{C}$ and convection heat transfer coefficient of $600 \mathrm{~W} / \mathrm{m}^{2}{ }^{\circ} \mathrm{C}$. Calculate the temperature at a radius of 1.25 cm and the heat lost per unit length 1 min after the cylinder is exposed to the environment.
11. A spherical hailstone $\left(\mathrm{k}=2.03 \mathrm{~W} / \mathrm{m}^{\circ} \mathrm{C}, \rho=920 \mathrm{~kg} / \mathrm{m}^{3}, \mathrm{C}=1945 \mathrm{~J} / \mathrm{kg}{ }^{\circ} \mathrm{C}\right)$ that is 8 mm in diameter is formed in a high altitude cloud at $-30^{\circ} \mathrm{C}$. If the stone begins to fall through warmer air at $5^{\circ} \mathrm{C}$, how long it takes before the outer surface begins to melt? What is the temperature of stone's center at this time, and how much energy (J) has been transferred to the stone? A convection heat transfer coefficient of $250 \mathrm{~W} / \mathrm{m}^{2 \circ} \mathrm{C}$.
